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# **JEST 4541**

# **ARTICLE IN PRESS**

## 27 August 2013

# Highlights

- Component-based estimation of response reduction factor (*R*).
  For RC moment framed buildings following Indian standards.
  Performance-based limit states at member and structure levels.
  Detailed modelling of an RC section's behaviour.
  Comparison of estimated
- Performance-based limit states at member and structure levels. Detailed modelling of an RC section's behaviour. Comparison of estimated R values with the code-specified value. Code-based value of R is non-conservative.

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# Performance-based evaluation of the response reduction factor for ductile RC frames

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#### ABSTRACT

Most seismic design codes today include the nonlinear response of a structure implicitly through a 'response reduction/modification factor' (R). This factor allows a designer to use a linear elastic force-based design while accounting for nonlinear behaviour and deformation limits. This research focuses on estimating the actual values of this factor for realistic RC moment frame buildings designed and detailed following the Indian standards for seismic and RC designs and for ductile detailing, and comparing these values with the value suggested in the design code. The primary emphases are in a component-wise computation of R, the consideration of performance-based limits at both member and structure levels, a detailed modelling of the RC section behaviour, and the effects of various analysis and design considerations on R. Values of R are obtained for four realistic designs at two performance levels. The results show that the Indian standard recommends a higher than actual value of R, which is potentially dangerous. This paper also provides other significant conclusions and the limitations of this study.

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## 1. Introduction

Today's seismic design philosophy for buildings, as outlined in 44 different codes and guidelines, such as ASCE7 [1], Eurocode 8 [2], 45 and IS 1893 [3], assumes nonlinear response in selected 46 components and elements when subjected to an earthquake of 47 the design intensity level. However, these codes and guidelines 48 49 do not explicitly incorporate the inelastic response of a structure in the design methodology. These designs are typically based on 50 the use of elastic force-based analysis procedures rather than dis-51 placement-based methods. The equivalent static lateral force 52 53 method, which has been used from the early days of engineering seismic design, is still the most preferable method to a structural 54 design engineer, because it is conceptually simple and less 55 56 demanding from a computational point of view. Most of the codes used for seismic deign of buildings use the concept of response 57 reduction to implicitly account for the nonlinear response of a 58 59 structure. In this approach, the design base shear  $(V_d)$  is derived 60 by dividing the elastic base shear demand  $(V_e)$ , which is obtained 61 using an elastic analysis considering the elastic pseudo-acceleration response spectrum (for 5% damping,  $S_{a,5}$ ), by a factor R: 62

$$V_d = \frac{V_e}{R} = \frac{S_{a,5}W}{R} \tag{1}$$

where W is the seismic weight of the structure. R is termed as the 66 "response reduction factor" in the Indian standard IS 1893 and 67 the "response modification coefficient" in ASCE7. In Eurocode 8 68 (EC8), the same factor is called the "behaviour factor". There are dif-69 70 ferences in the way the response reduction factor (R) is specified in different codes for different kinds of structural systems. The objec-71 tive of the present study is to obtain *R* for reinforced concrete (RC) 72 regular frame structures designed and detailed as per Indian stan-73 dards IS 456 [4], IS 1893 [3] and IS 13920 [5]. Existing literature 74 in this area do not provide any specific basis on which a value of 75 76 5.0 is assigned for such frames in the Indian standard IS 1893. The present work takes a rational approach in determining this fac-77 tor for regular RC framed building structures, by considering differ-78 ent acceptable performance limit states. Most of the past research 79 efforts in this area have focused on finding the ductility component 80 of the response reduction factor for single-degree-of-freedom 81 (SDOF) systems considering the local seismicity in different parts 82 of the world. Although some researchers have worked on various 83 components of the response reduction factor in detail, the 84 acceptable limit states considered in these works have been 85 assumed arbitrarily. The work presented in this paper focuses on 86 a component-wise determination of the R factor for RC frames 87 designed and detailed as per Indian standard specifications, consid-88 ering performance limits based on their deformation capacity. 89

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## 90 2. Components of *R* and design standards

Commonly, the response reduction factor is expressed as a function of various parameters of the structural system, such as strength, ductility, damping and redundancy [6–8]:

94  
96 
$$R = R_s R_u R_{\varepsilon} R_R$$
 (2

where  $R_s$  is the strength factor,  $R_{\mu}$  is the ductility factor,  $R_{\xi}$  is the damping factor, and  $R_R$  is the redundancy factor. The strength factor  $(R_s)$  is a measure of the built-in overstrength in the structural system and is obtained by dividing the maximum/ultimate base shear  $(V_u)$  by the design base shear  $(V_d)$ .

$$\mathbf{A} \qquad R_{\rm s} = \frac{V_u}{V_d} \tag{3}$$

It should be noted that the strength factor in a structure depends on 105 various factors, such as the safety margins specified in the code that 106 107 is used to design the structure. Even with the same design code,  $R_s$ 108 becomes subjective to the individual designer's choice of a section 109 depending on the demand, because the section provided for a mem-110 ber is never exactly as per the design requirements. For example, 111 the same section will be provided for, say, external columns over 112 two to three stories, although the design requirement usually varies 113 for these. Additionally, the reinforcements provided are typically slightly more than the required due to the availability of discrete re-114 115 bar sizes. These conservative decisions imparted through a de-116 signer's choice adds to  $R_s$ . Other parameters which contribute to 117  $R_{\rm s}$ , are the different partial safety factors. The ductility factor  $(R_{\mu})$ is a measure of the global nonlinear response of a structural system 118 119 in terms of its plastic deformation capacity. It is measured as the ra-120 tio of the base shear considering an elastic response  $(V_e)$  to the max-121 imum/ultimate base shear considering an inelastic response  $(V_{\mu})$ . 122 The different base shear levels used to define these two components 123  $(R_s \text{ and } R_u)$  are illustrated in Fig. 1. In the last three decades, significant work has been carried out to establish the ductility factor 124 based on SDOF systems subjected to various types of ground mo-125 tions. Among these, the works by Newmark and Hall [9], Riddell 126 127 and Newmark [10], Vidic et al. [11], and Krawinkler and Nassar [12] are significant and are frequently referred to. For a detailed re-128 view of research conducted in this area, the reader is requested to 129 130 refer to the paper by Miranda and Bertero [13]. In this study, the 131  $R-\mu-T$  relationships developed by Krawinkler and Nassar [12] are 132 used. These relationships are based on a detailed statistical study of the response of inelastic SDOF systems (with 5% damping) on 133 rock or stiff soil subjected to strong motion records of the western 134

United States. As per Krawinkler and Nassar [12], the ductility factor can be expressed as

$$R_{\mu} = [c(\mu - 1) + 1]^{1/c} \tag{4}$$

where  $\mu$  is the displacement ductility. The parameter *c* depends on the elastic vibration period (*T*) and the post- to pre-yield stiffness ratio ( $\alpha$ ) of the inelastic SDOF system:

$$c = \frac{T^a}{1+T^a} + \frac{b}{T} \tag{5}$$
 145

*a* and *b* are regression parameters, based on  $\alpha$ .  $R_{\mu}$  values based 146 on Eqs. (4 and 5) are plotted in Fig. 2, which directly provides the 147 ductility factor  $(R_{\mu})$  corresponding to a specific displacement duc-148 tility ( $\mu$ ). The ductility capacity ( $\mu = \Delta_u |_{\mu} \Delta_y$ ) is obtained from the 149 bilinearised pushover curve, for the deformation limits corre-150 sponding to the selected performance level of failure. The  $R-\mu-T$ 151 relationship translates this displacement ductility capacity onto 152 the force axis as the  $R_{\mu}$  factor. From Fig. 1, it should be understood 153 that the elastic force demand on the system  $(V_e)$  can be reduced by 154 the factor  $R_{\mu}$  owing to the inelastic displacement capacity (or  $\mu$ ) 155 available with the system. The damping factor  $(R_{*})$  accounts for 156 the effect of "added" viscous damping and is primarily applicable 157 for structures provided with supplemental energy dissipating 158 devices. Without such devices, the damping factor is generally as-159 signed a value equal to 1.0 and is excluded from the determination 160 of the response reduction factor for the purpose of force-based de-161 sign procedures [6,8]. RC structural systems with multiple lines of 162 lateral load resisting frames are generally in the category of redun-163 dant structural systems, as each of the frames is designed and de-164 tailed to transfer the earthquake induced inertia forces to the 165 foundation. For these systems, the lateral load is shared by differ-166 ent frames depending on the relative (lateral) stiffness and 167 strength characteristics of each frame. Together, frames aligned 168 in the same direction form a redundant parallel system, and the 169 reliability of the system, theoretically, is more than or equal to 170 each frame's individual reliability. The reliability of the system is 171 higher for structures with multiple lines of frames with uncorre-172 lated characteristics, and the system reliability is reduced to the 173 individual frame's reliability when the resistance parameters are 174 perfectly correlated. Following the conservative suggestion of 175 ASCE7, a redundancy factor  $R_R = 1.0$  is used in this study. 176

The typical value of the response reduction factor specified in different international standards varies depending on the type of structural system as well as the ductility class of the structure under consideration. For regular RC frames, values of *R* as specified in IS 1893 (Part 1), EC8 and ASCE7 are provided in Tables 1–3, respec-



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#### Table 1

Values of *R* for RC framed structures, as per IS 1893.

| Structural system                      | R   |
|--|-----|
| Ordinary moment resisting frame (OMRF) | 3.0 |
| Special moment resisting frame (SMRF)  | 5.0 |

#### Table 2

Values of the 'behaviour factor' for RC framed structures, as per EC8.

| Structural system            | Behaviour factor    |
|------------------------------|---------------------|
| Medium ductility class (DCM) | $3.0V_u/V_y = 3.90$ |
| High ductility class (DCH)   | $4.5V_u/V_y = 5.85$ |

#### Table 3

Values of R for RC framed structures, as per ASCE7.

| Structural system            | Response modification coefficient, <i>R</i> | System overstrength factor, $arOmega_0$ |
|------------------------------|---|---|
| Ordinary moment<br>frame     | 3.0   | 3.0                                     |
| Intermediate<br>moment frame | 5.0   | 3.0                                     |
| Special moment<br>frame      | 8.0   | 3.0                                     |

182 tively. IS 1893 gives a value of R equal to 3.0 and 5.0 for ordinary 183 and special RC moment resisting frames (OMRF and SMRF). The 184 SMRF needs to follow the ductile detailing requirements of IS 13920. IS 1893 does not explicitly segregate the components of R 185 in terms of ductility and overstrength. Also, it does not specify 186 any reduction in the response reduction factor on account of any 187 irregularity (vertical or plan-irregularity) in the framing system. 188 189 EC8 gives the behaviour factor (q) for regular RC framed structures 190 for two ductility classes: medium and high (DCM and DCH). The 191 ductility and overstrength components are properly incorporated 192 in the formulation of this factor. The ratio  $V_u/V_v$  in Table 2 represents the overstrength component of the behaviour factor, where 193 194  $V_{\nu}$  is the base shear at the first yield. For multistory multibay frames, this ratio is specified in EC8 as 1.30 making the behaviour 195 factor equal to 3.90 and 5.85 for DCM and DCH, respectively. For 196 irregular buildings, the behaviour factor is reduced by 20%. ASCE7 197 198 categorises RC frames into three ductility classes (Table 3). It 199 should be noted that although this coefficient is applied for obtaining the design base shear for a structure or framing system, the de-200 sign of individual members exclude the strength and redundancy 201 202 components of R. The design member forces are therefore obtained 203 by multiplying the member forces corresponding to the design 204 shear force with the system overstrength ( $\Omega_0$ ). No such specifica-205 tion exists in IS 1893 or EC8.

#### 206 **3. Structural performance limits**

207 The definition of the response reduction factor, R, is integrated 208 to the selected performance limit state of the structure. The Indian standard IS 1893 does not specify the limit state corresponding to 209 which values of *R* are recommended in this code. However, based 210 211 on the design philosophy outlined in the initial sections of this 212 seismic design guideline (and comparing with the R values in other codes), it can be safely assumed that these values are based on the 213 ultimate limit state of the structure. Quantitative definition of the 214 215 ultimate limit state of a structure is also not provided in this code. 216 The selection and the definition of a performance limit state to ob-217 tain R needs to be looked into in detail, particularly considering

#### Table 4

Deformation limits for different performance levels, as per ATC-40.

|                                       | Performance level      |                   |                |  |
|---------------------------------------|------------------------|-------------------|----------------|--|
|                                       | Immediate<br>occupancy | Damage<br>control | Life<br>safety | Structural<br>stability  |
| Maximum<br>interstorey drift<br>ratio | 0.01                   | 0.01-0.02         | 0.02           | 0.33 <i>V</i> <sub><i>i</i></sub> / <i>P</i> <sub><i>i</i></sub> |

similar specifications in newer design standards and guidelines around the world.

Over the last 10–15 years, concepts related to the performancebased seismic design (PBSD) philosophy has gradually entered into the earthquake engineering state of the practice. A PBSD guideline typically provides clear definitions of multiple performance limit states of various types. In PBSD terminology, the limit states are typically known as structural 'performance levels', which in combination with seismic 'hazard levels' define the 'performance objective' for a structure. The performance levels are defined based on the structure type and its intended functions. Different PBSD guidelines, for example ATC-40 [14] or FEMA-356 [15], have provided slightly different definitions (and names) of the performance limit states. Broadly, the performance limits can be grouped into two categories: global/structural limits and local/element/component limits.

The global limits typically include requirements for the vertical 234 load capacity, lateral load resistance and lateral drift. For example, 235 the various performance levels in ATC-40 [14] are specified in 236 terms of the maximum interstorey drift ratio (Table 4). Among 237 these performance levels, the Structural Stability level corresponds 238 to the ultimate limit state of the structure, which can be used for 239 obtaining R (more specifically,  $R_{\mu}$ ) for a selected structure. One 240 should note that the same performance limit indicating impending 241 collapse is termed as Collapse Prevention in some other docu-242 ments, such as FEMA-356. For this level, the maximum total inter-243 storey drift ratio in the *i*th story should not exceed  $0.33V_i/P_i$ , where 244  $V_i$  is the total lateral shear force demand in the *i*th storey and  $P_i$  is 245 the total gravity load acting at that storey. The local performance 246 levels are typically defined based on the displacement, rotation 247 or acceleration responses of different elements (beams, columns, 248 shear walls, floors, etc.). The limits on the response of structural 249 elements, such as beams and columns, are many times governed 250 by non-structural and component damages as well. For example, 251 Table 5 provides the 'local' deformation limits specified by 252 ATC-40 in terms of plastic hinge rotations of beam elements in a 253 RC moment resisting frame. Table 6 provides similar limiting 254 values of column rotation for different performance levels. These 255 limits are for flexural failures of an element. Therefore, to use these 256 limits, one should ensure that the failure of a member/structure is 257 governed by flexural demands, and shear failure, for example, does 258 not take place before these rotational limits are reached. The 259 capacity design philosophy, which is incorporated in most seismic 260 261 design codes today, ensures a preferred failure hierarchy. The shear

| Table 5                              |                                       |
|--------------------------------------|---------------------------------------|
| Plastic rotation limits for RC beams | controlled by flexure, as per ATC-40. |

|   |                  |                               | Immediate<br>occupancy | Life<br>safety | Structural<br>stability |
|---|------------------|-------------------------------|------------------------|----------------|-------------------------|
| $rac{ ho- ho'}{ ho_{bal}}$   | Trans.<br>reinf. | $\frac{V}{b_w d \sqrt{f'_c}}$ | Plastic rotation limi  | t              |                         |
| ≼0  | С                | ≼3                            | 0.005                  | 0.020          | 0.025                   |
| ≼0  | С                | ≥6                            | 0.005                  | 0.010          | 0.020                   |
| C indicates that transverse reinforcement meets the criteria for ductile detailing. |                  |                               |                        |                |                         |

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#### Table 6

Plastic rotation limits for RC columns controlled by flexure, as per ATC-40.

|                           |                  |                               | Immediate<br>occupancy  | Life<br>safety          | Structural<br>stability |
|---------------------------|------------------|-------------------------------|-------------------------|-------------------------|-------------------------|
| $\frac{P}{A_{\rm g}f_c'}$ | Trans.<br>reinf. | $\frac{V}{b_w d \sqrt{f'^c}}$ | Plastic rotation lim    | it                      |                         |
| ≤0.1<br>≤0.1<br>> 0.4     | C<br>C           | <3<br>≥6<br><3                | 0.005<br>0.005<br>0.000 | 0.010<br>0.010<br>0.005 | 0.020<br>0.015<br>0.015 |
| ≥ 0.4<br>≥ 0.4            | c                | ≥6                            | 0.000                   | 0.005                   | 0.010                   |

C indicates that transverse reinforcement meets the criteria for ductile detailing.

detailing provisions specified in IS 13920 ensures that shear failure 262 263 does not initiate before the formation flexural plastic hinges at 264 member ends. On the basis of these background information, it is 265 decided to consider an ultimate limit state based on flexural failure 266 at both local and global levels in this paper. Due to the lack of such detailed definition of any ultimate limit state in the Indian stan-267 268 dard IS 1893, the Structural Stability performance level of ATC-40 is used here, both at the structure level and at the member levels. 269 270 In addition, actual member plastic rotation capacities, for individ-271 ual members, are also considered in obtaining R for real RC frames.

## **4. Description of the structural systems considered**

The structural systems considered for this study are four typical 273 symmetric-in-plan RC frame structures having two-, four-, eight-274 and 12-storied configurations, intended for a regular office build-275 ing in the seismic zone IV as per IS 1893 [3]. The seismic demands 276 on these buildings are calculated following IS 1893. The RC design 277 for these buildings are based on IS 456 guidelines [4] and the (seis-278 279 mic) ductile detailing of the RC sections are based on IS 13920 provisions [5]. The study building is assumed to be located in zone IV, 280 281 which is the second most seismically intensive zone covering a 282 large part of the country including the national capital New Delhi 283 and several other sate capitals. The design base shear for a building 284 is derived as: 285

$$V_d = \frac{ZIS_a}{2Rg}W$$
(6)

where Z denotes the zone factor (= 0.24 for zone IV), I is the struc-288 289 ture's importance factor (= 1 for these buildings), R = 5.0 for ductile or 'special' moment resisting frames (SMRF), S<sub>a</sub> is the spectral accel-290 291 eration, and W is the seismic weight of the structure. All study struc-292 tures have the same plan arrangement with four numbers of bays (6.0 m each) in both directions as shown in Fig. 3. The floor to floor 293 height is 4.0 m for all the storeys and the depth of foundation is 294 295 3.0 m. A typical elevation (for the 4-storied frame) is shown in 296 Fig. 4. These moment resisting frame structures of different heights are selected to typically represent "short", "medium" and "long" 297 period structures. Further details on these planar frames, such as to-298 tal height (from the foundation level), fundamental period, total 299 300 seismic weight, and design base shear, are provided in Table 7. Fig. 5 shows the fundamental periods of these four frames on the 301 302 5% damping pseudo-acceleration design spectrum specified in IS 303 1893 for a 'medium' soil condition in Zone IV [3]. The fundamental 304 periods of the structures, presented in Table 7, are calculated based 305 on the empirical formula recommended in IS 1893. The RC frames 306 are designed with M25 grade concrete (having 28 days characteristic cube strength of 25 MPa) and Fe415 grade reinforcements (having a 307 characteristic yield strength of 415 MPa) [4]. 308

As mentioned earlier, the selected structural design for a building is not a unique solution available for the demands calculated. Based on the same demand, different designers may select differ-



Fig. 3. Structural arrangement of the four buildings in plan.



Fig. 4. Elevation of the four-story RC frame structure.

Table 7

| Details of the | RC frames | considered | for the | case | study |
|----------------|-----------|------------|---------|------|-------|
|----------------|-----------|------------|---------|------|-------|

| Frame   | Height (m)                   | $T_d(s)$                       | W(kN)                          | $A_h = V_d/W$                        | $V_d$ (kN)               |
|---|------------------------------|--------------------------------|--------------------------------|--------------------------------------|--------------------------|
| 2-Storey<br>4-Storey<br>8-Storey<br>12-Storey | 11.0<br>19.0<br>35.0<br>51.0 | 0.453<br>0.683<br>1.08<br>1.43 | 4650<br>7770<br>13800<br>19800 | 0.0600<br>0.0478<br>0.0302<br>0.0228 | 279<br>371<br>416<br>451 |
|   |                              |                                |                                |                                      |                          |

ent design solutions. The RC design solutions selected for these 312 buildings are based on common practices adopted by design engi-313 neers. For example, in a planar frame, all the internal columns in a 314 storey are chosen to have the same section and similarly the beams 315 in a specific floor. The column sections remain the same over two 316 to three storeys depending on the building height. The Indian stan-317 dards do not specifically enforce a strong-column-weak-beam 318 (SCWB) behaviour. However, considering the practice followed in 319 most countries, the strong-column-weak-beam requirement (in 320 terms of beam and column moment capacities) is considered in 321 these designs. The RC section details ensuring the strong-col-322 umn-weak-beam behaviour are provided in Table 8. An alternative 323 set of designs are also obtained without considering the strong-col-324 umn-weak-beam requirement in selecting the sections, which is 325

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Fig. 5. 5% damping response spectrum for 'medium' soil in zone IV, as per IS 1893.

discussed in detail in Section 7.3. The response reduction factor (R) is obtained for both sets of designs.

#### 328 5. Modelling of RC members

Estimation of R values of these study frames depends signifi-329 330 cantly on how well the nonlinear behaviour of these frames are 331 represented in analyses. Since *R* values are estimated on the basis of nonlinear static pushover analyses, the focus of the modelling 332 scheme employed here is to capture the nonlinear static behaviour 333 334 of the RC frame members. A few critical aspects of the modelling 335 scheme adopted in this work are described in this section. The non-336 linear behaviour of the frame depends primarily of the moment-337 rotation behaviour of its members, which in turn depends on the 338 moment-curvature characteristics of the plastic hinge section and the length of the plastic hinge. These two parameters also de-339 fine the 'component' level performance limit in terms of the plastic 340 341 rotation capacity. In addition to these two aspects, the other important aspect that is discussed in this section is the initial stiff-342 343 ness of a member which affects the force-deformation relation in 344 the 'linear elastic' zone.

# 345 5.1. Moment-curvature characteristics of RC sections

The moment-curvature  $(M-\phi)$  characteristics of various RC sections are developed using the widely used Kent and Park model

#### Table 8

| RC section details for the s | tudy frames (with the | SCWB design criterion |
|------------------------------|-----------------------|-----------------------|
|------------------------------|-----------------------|-----------------------|

[16], which considers the confinement effect of the (closed) transverse reinforcements. Various other analytical models for this, that are frequently referred to in literature, are those proposed by Mander et al. [17], Baker and Amarakone [18], Roy and Sozen [19], Soliman and Yu [20], Sargin et al. [21], Sheikh and Uzumeri [22], and Saatcioglu and Razvi[23]. Based on the results of experiments conducted on a large number of beam-column joints of different dimensions, Sharma et al. [24] concluded that response estimations using the Kent and Park model closely matched the experimental results in the Indian scenario. The ductile design provisions of IS 13920 require that transverse reinforcements in beams and columns should be able to confine the concrete core. Considering this, the Kent and Park model for confined concrete is used for the concrete within the stirrups, and unconfined concrete characteristics, following again the Kent and Park guidelines, are assigned to the cover concrete. Spalling of the concrete cover is also modelled in case the strain outside the confined core exceeds the ultimate compressive strain of unconfined concrete. Priestley [25] prescribed an ultimate concrete strain (in compression) for unconfined concrete,  $\epsilon_{cu}$  = 0.005, which is adopted in this work. The ultimate compressive strain of concrete confined by transverse reinforcements ( $\epsilon_{cc}$ ) as defined in ATC-40 is adopted in this work to develop the  $M_{-\phi}$  characteristics of plastic hinge sections:

$$\epsilon_{cc} = 0.005 + 0.1 \frac{\rho_s f_y}{f_{c}} \leqslant 0.02$$
 (7)

In order to avoid the buckling of longitudinal reinforcement bars in between two successive transverse reinforcement hoops, the limiting value of  $\epsilon_{cc}$  is restricted to 0.02. Other researchers, for example, Priestley<sup>[25]</sup>, also proposed similar expressions for the ultimate compressive strain of confined concrete. A typical  $M-\phi$  curve for a RC beam section under hogging (tension at top) moments for the four-storey frame is shown in Fig. 6. Considering the presence of rigid floor diaphragms, the effects of axial force on a beam's  $M-\phi$ behaviour are disregarded. However, these effects are included while obtaining the  $M_{-\phi}$  relation for the column sections. Fig. 7 shows a typical  $M-\phi$  plot for an exterior column section of the four-storey frame, for different levels of axial force P (normalised to its axial force capacity,  $P_{uz}$ ). It is observed that there is a drop in the  $M_{-\phi}$  curves for both beam and column sections after the peak moment capacity is reached. This is on account of the spalling of the concrete cover when the strain in concrete in that region exceeds the ultimate strain for unconfined concrete ( $\epsilon_{cu}$  = 0.005). This is more prominent for column sections than beam sections and this drop becomes more significant as  $(P/P_{uz})$  is increased.

| Frame     | Members | Floors | Width<br>(mm) | Depth<br>(mm) | Reinforcement details   |
|-----------|---------|--------|---------------|---------------|---|
| 2-Storey  | Beams   | 1-2    | 250           | 500           | $[3 - 25\Phi + 2 - 20\Phi](top) + [2 - 25\Phi + 1 - 20\Phi]$ (bottom) |
|           | Columns | 1-2    | 450           | 450           | 8 – 25 $\Phi$ (uniformly distributed)                                 |
| 4-Storey  | Beams   | 1-4    | 300           | 600           | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                           |
| -         | Columns | 1-4    | 500           | 500           | $12 - 25\Phi$ (uniformly distributed)                                 |
| 8-Storey  | Beams   | 1-4    | 300           | 600           | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                           |
| ·         | Columns | 1-4    | 600           | 600           | $12 - 25\Phi$ (uniformly distributed)                                 |
|           | Beams   | 5-8    | 300           | 600           | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                           |
|           | Columns | 5-8    | 500           | 500           | $12-25\Phi$ (uniformly distributed)                                   |
| 12-Storey | Beams   | 1-4    | 300           | 650           | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                           |
|           | Columns | 1-4    | 750           | 750           | $12 - 25\Phi$ (uniformly distributed)                                 |
|           | Beams   | 5-8    | 300           | 600           | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                           |
|           | Columns | 5-8    | 600           | 600           | $12-25\Phi$ (uniformly distributed)                                   |
|           | Beams   | 8-12   | 250           | 550           | $6 - 25\Phi$ (top) + $3 - 25\Phi$ (bottom)                            |
|           | Columns | 8-12   | 500           | 500           | $12-25\Phi$ (uniformly distributed)                                   |

 $\Phi$  is the diameter of a rebar.

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 $L_p = 0.08L + 0.022 f_{va} d_{bl}$ 



425

(9)



**Fig. 6.** Sample M- $\phi$  characteristics of a beam section of the four-storey frame under 'hogging' bending moment.



**Fig. 7.** Sample M- $\phi$  characteristics of a column (external) section of the four-storey frame.

#### 393 5.2. Plastic hinge characteristics

397

The plastic rotation capacity  $(\theta_p)$  in a reinforced concrete member depends on the ultimate curvature  $(\phi_u)$  and the yield curvature  $(\phi_v)$  of the section and the length of the plastic hinge region  $(L_p)$ :

$$\theta_p = (\phi_u - \phi_v) L_p \tag{8}$$

Park and Paulay [26] reported that various researchers had proposed different empirical models to predict the length of a plastic hinge. One of the most widely used models for  $L_p$  is that proposed by Priestley [25]:

| where <i>L</i> is the distance from the critical section to the point of con-              | 407 |
|--|-----|
| traflexure, <i>f<sub>va</sub></i> is the yield strength (in MPa) of longitudinal bars hav- | 408 |
| ing a diameter $d_{bl}$ . For a moment-resisting frame, where lateral                      | 409 |
| loads (for example, seismic) are predominant, the point of contra-                         | 410 |
| flexure typically occurs close to the mid-span of a member. The                            | 411 |
| plastic rotation capacities of frame members of the four study                             | 412 |
| structures are computed using Equations (8 and 9), assuming the                            | 413 |
| points of contraflexure to be at the mid-span of members. Sample                           | 414 |
| plastic rotation capacities computed for some typical members of                           | 415 |
| the 12-storey frame (for which Table 8 provides the section details)                       | 416 |
| are given in Table 9. These capacities are computed for purely flex-                       | 417 |
| ural conditions, without the effects of any axial load. The plastic                        | 418 |
| rotation capacities of the column elements for different (norma-                           | 419 |
| lised) axial load levels are provided in Table 10. As suggested by                         | 420 |
| many previous researchers for this type of framed structures, the                          | 421 |
| lumped plasticity model, with plastic hinge formation possibility                          | 422 |
| at both ends of a member, is used for nonlinear static pushover                            | 423 |
| analyses.  | 424 |

#### 5.3. Initial stiffness of RC members

Appropriate modelling of the initial stiffness of RC beams and 426 columns is one of the important aspects in the performance evalu-427 ation of reinforced concrete frames. The initial stiffness of mem-428 bers significantly affects the yield displacement of a frame 429 structure. Consequently, the displacement ductility  $(\mu)$ , which is 430 the ratio of the ultimate to the yield displacement, is also greatly 431 affected by the initial stiffness of members adopted in the nonlin-432 ear static analysis. The stiffness of a reinforced concrete section 433 may be determined as a function of its material properties, rein-434 forcement quantities, and induced stress and deformation levels. 435 For a primarily flexural member, the effective stiffness can be com-436 puted by considering (a) the variation of bending moment along its 437 length and (b) the 'cracked' moment of inertia of the transformed 438 section. Various other parameters, that affect the force deforma-439 tion characteristics of a cracked concrete section, are the deforma-440 tion due to shear cracking, partial reinforcement slip from adjacent 441 joints, effect of aggregate interlock, dowel action of reinforcement 442 bars, tension stiffening, etc. The exact estimation of initial stiffness 443 of each individual member incorporating all of these effects be-444 comes impractical due to the complexity involved in modelling 445 and the increased demand on computation. Considering this, it is 446 suggested in both ATC-40 [14] and FEMA-356 [15] to use the fol-447 lowing values for initial stiffness of RC members:  $0.5E_c I_g$ ,  $0.7E_c I_g$ 448 and  $0.5E_{clg}$  for beams, columns under compression, and columns 449 under tension, respectively.  $E_c$  is the modulus of elasticity of con-450 crete and  $I_{\varphi}$  is the moment of inertia of the 'gross section'. Since 451 a column may be subjected to both compression and tension in 452 alternate cycles during earthquakes, an average value of  $0.6E_cI_g$  is 453

| Table 9                                |               |                    |            |
|--|---------------|--------------------|------------|
| Plastic rotation capacities of the fra | me sections o | of 12-storev frame | structure. |

| Member | Action     | Size (mm)        | Clear span (mm) | $L_p$ (mm) | $\phi_y$ (rad/mm) | $\phi_u$ (rad/mm) | $\theta_p$ (rad) |
|--------|------------|------------------|-----------------|------------|-------------------|-------------------|------------------|
| Beam   | + <i>M</i> | 300 × 650        | 5250            | 438        | 8.93E-06          | 2.48E-04          | 0.105            |
| Beam   | -M         | $300 \times 650$ | 5250            | 438        | 1.08E-05          | 1.00E-04          | 0.0391           |
| Beam   | +M         | 300 	imes 600    | 5400            | 444        | 9.56E-06          | 2.48E-04          | 0.106            |
| Beam   | -M         | 300 	imes 600    | 5400            | 444        | 1.22E-05          | 1.01E-04          | 0.0392           |
| Beam   | +M         | 250 	imes 550    | 5500            | 448        | 1.13E-05          | 2.47E-04          | 0.106            |
| Beam   | -M         | $250\times 550$  | 5500            | 448        | 1.48E-05          | 8.41E-05          | 0.0311           |
| Column | ±Μ         | $750\times750$   | 3350            | 362        | 7.57E-06          | 1.28E-04          | 0.0435           |
| Column | ±M         | 600 	imes 600    | 3400            | 364        | 1.06E-05          | 1.25E-04          | 0.0418           |
| Column | $\pm M$    | $500\times500$   | 3450            | 366        | 1.40E-05          | 1.23E-04          | 0.0398           |

+*M* indicates 'sagging' moment (causing tension at the bottom of a beam). The longitudinal bar is of 25 mm diameter and the yield strength is 415 MPa.  $\theta_p$  for column sections are based only on flexural actions.

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| Table  | 10   |         |    |        |         |          |            |     |     |           |       |
|--------|------|---------|----|--------|---------|----------|------------|-----|-----|-----------|-------|
| Axial  | load | effects | on | column | plastic | rotation | capacities | for | the | 12-storey | frame |
| struct | ure. |         |    |        |         |          |            |     |     |           |       |

| Axial load $P_u/P_{uz}$ | Plastic rotation | Plastic rotation capacity, $\theta_p$ (rad) |               |  |  |  |  |  |
|-------------------------|------------------|---|---------------|--|--|--|--|--|
|                         | Column           | Column                                      | Column        |  |  |  |  |  |
|                         | $(750\times750)$ | (600	imes 600)                              | (500	imes500) |  |  |  |  |  |
| 0.0                     | 0.0435           | 0.0418                                      | 0.0398        |  |  |  |  |  |
| 0.1                     | 0.0249           | 0.0272                                      | 0.0343        |  |  |  |  |  |
| 0.2                     | 0.0178           | 0.0236                                      | 0.0304        |  |  |  |  |  |
| 0.3                     | 0.0148           | 0.0196                                      | 0.0224        |  |  |  |  |  |
| 0.4                     | 0.0115           | 0.0140                                      | 0.0174        |  |  |  |  |  |
| 0.5                     | 0.00838          | 0.0111                                      | 0.0159        |  |  |  |  |  |
| 0.6                     | 0.00657          | 0.0101                                      | 0.0146        |  |  |  |  |  |
| 0.7                     | 0.00598          | 0.00911                                     | 0.0126        |  |  |  |  |  |
| 0.8                     | 0.00538          | 0.00822                                     | 0.0122        |  |  |  |  |  |
| 0.9                     | 0.00494          | 0.00791                                     | 0.0118        |  |  |  |  |  |

454 adopted as the initial stiffness for all column elements, following455 ATC-40's suggestion.

# 456 **6. Nonlinear static pushover analysis of RC frames**

457 Nonlinear static pushover analyses (NSPA) of the four study
458 frames are performed to estimate their overstrength and global
459 ductility capacity, which are required for computing *R* for each
460 frame. The equivalent lateral force distribution adopted for this
461 pushover analysis is as suggested in IS 1893:

$$Q_{i} = V_{d} \frac{W_{i} h_{i}^{2}}{\sum_{i=1}^{n} W_{i} h_{i}^{2}}$$
(10)

where  $Q_i$  is the equivalent lateral force on the *i*th floor,  $W_i$  the seis-465 mic weight of the *i*th floor,  $h_i$  the height up to the *i*th floor, and *n* is 466 467 the total number of storeys. More complex, vibration mode/period-468 dependent distributions have been suggested in other codes, such 469 as ASCE7: however, the distribution as per IS 1893 is used in this 470 study considering its overwhelming use in India. The effect of 471 adopting other lateral load distributions in NSPA on the R factor is 472 discussed in detail in Section 7.6. Owing to the rigid floor diaphragm in every floor and the symmetric-in-plan configuration 473 avoiding any torsional motion, only a two-dimensional pushover 474 analysis of a single frame is performed for these evaluations. 475

476 The NSPA are performed using the DRAIN-2DX analysis software [27]. The intermediate frames having maximum gravity load 477 478 effects are considered for the pushover analysis. All beam and col-479 umn members are modelled using the 'plastic hinge beam column element (Type 02)' available in DRAIN-2DX. For beam members, 480 the axial load effects are ignored considering the rigid floor dia-481 482 phragm effect. For column members, the effect of axial loads on plastic hinges are considered using a *P*–*M* interaction diagram for 483 each different RC section. A typical P-M interaction plot for the 484  $500 \times 500$  column section is shown in Fig. 8. No shear hinge forma-485 tion is considered in these analyses, as the various design and 486 detailing provisions specified in IS 13920 eliminate the possibility 487 of such a failure. The joint panel zones are assumed to be rigid and 488 489 strong enough to avoid any premature failure before forming a 490 mechanism by the failure of other members, following again the capacity design concepts adopted in IS 13920. 491

The design gravity loads are applied before applying the incremental lateral forces. The gravity loads are applied as distributed element loads based on yield line theory and concentrated loads from secondary beams. First, a static analysis is performed for the full gravity load in a single step. The state of the structure from this analysis is saved and subsequently the static pushover analysis is conducted starting from this state of the structure. For the non-



**Fig. 8.** Sample *P*–*M* interaction for an external column section of the four-storey frame.

linear static analysis, both the load control and the displacement control strategies are adopted. The analysis is load controlled up to the first yield and displacement controlled thereafter. The inclusion of  $P_{\overline{1}} \varDelta$  effects changes the lateral force-deformation behaviour of a frame. Section 7.5 discusses in detail the effects of including (and, of not including) geometric nonlinearity in NSPA on the computed *R* values. The output of a nonlinear static analysis is generally presented in the form of a 'pushover curve', which is typically the base shear vs. roof displacement plot. Pushover curves obtained from NSPA performed on the two-, four-, eight- and 12storey frames are shown in Figs. 9-12, respectively. The interstorey drift ratio values are checked at every load/displacement increment against the performance limits defined. Similarly at the member level, the plastic rotations for individual components are also checked against the respective limits based on the induced load levels. The performance level is marked on the pushover curve, when for the first time any of these limits is reached.

## 7. Computation of *R* for the study frames

As mentioned earlier in Section 3, two performance limits are 517 considered in the computation of *R* for the study frames. The first 518 one (Performance Limit 1 or PL1) corresponds to the Structural Sta-519 bility limit state defined in ATC-40, which is exactly the same or 520 very close to the ultimate limit states defined in subsequent seis-521 mic design/assessment guidelines, such as FEMA-356. This limit 522 state is defined both at the storey level (in terms of the maximum 523 interstorey drift ratio) and at the member level (in terms of the 524 allowable plastic hinge rotation at member ends). The second limit 525





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Fig. 10. Pushover curves for the four-storey frame.







Fig. 12. Pushover curves for the 12-storey frame.

state (*Performance Limit 2* or PL2) is based on plastic hinge rotation
 capacities that are obtained for each individual member depending
 on its cross-section geometry, as discussed in Section 5.2.

In order to compute the different components of the response
reduction factor, various parameters, such as roof displacement,
base shear, interstorey drift ratio, and member plastic rotation – pertaining to both the yield and the ultimate limit states of a structure –
are obtained from the NSPA. The limit state of 'yield' of a structure, in
this paper, is based on a bilinearisation of the base shear vs. roof

displacement ('pushover') plot, considering equal areas under the<br/>actual and the approximating curves. A similar scheme of bilineari-<br/>sation was adopted in many previous studies on performance-based<br/>seismic design [6,28,29]. This section first provides the results of<br/>computing the *R* factor considering both PL1 and PL2, and then dis-<br/>cusses the effect of several considerations in the methodology<br/>adopted on the computed values of *R*.535<br/>538

#### 7.1. Computation of R for PL1 542

The global performance limit for PL1 is defined by a maximum 543 interstorey drift ratio of  $0.33V_i/P_i$  (Table 4). For the four study 544 structures, where the maximum  $V_i$  (at the base) is around 6% of 545 the  $P_i$ , this limit is found to be 0.02. At the component level, based 546 on the sectional configuration as well as the induced load level 547 (normalised with respect to respective section capacities), the plas-548 tic rotation limits of individual member is derived from the values 549 given in Tables 5 and 6, for beam and column elements, respec-550 tively. These three quantities defining both the structure level 551 and component level limits are monitored continuously at each 552 load/displacement increment during the NSPA, and the analysis 553 is terminated when one of the limit states is reached. Figs. 9-12 554 present the pushover plots for the study frames for both including 555 and excluding  $P_{-1}$  effects in the analysis. Points marked 'PL1' in 556 these base shear vs. roof displacements curves mark the first in-557 stants of reaching a PL1 limit state, as described earlier. PL1 can 558 thus be due to reaching the specified maximum interstorey drift 559 ratio or the plastic rotation at member ends. For each of the study 560 frames, Table 11 shows which of these limit states is governing. 561 Parameters necessary for the computation of R – the maximum 562 base shear up to the specific performance limit  $(V_u)$ , ultimate roof 563 displacement  $(\Delta_u)$ , yield base shear  $(V_y)$  and the yield roof dis-564 placement  $(\Delta_y)$  – are obtained from the pushover plots (or from 565 their bilinear approximations). Table 11 also presents the values 566 of these parameters for each study frame, along with the ductility 567 ratio ( $\mu$ ) and the overstrength ( $\Omega$ ) derived from these parameters. 568 The response reduction factor (R) computed on the basis of these 569 parameters are shown in Table 12 for the four frames, along with 570 a component-wise break-up for *R*. A value of  $R_R$  = 1.0 is adopted 571 as in these calculations, based on ASCE7's recommendation for 572 similar parallel load-resisting frames. 573

The R values range from 4.23 to 4.96 for the four frames consid-574 ered, and are all lesser than the IS 1893 specified value of R (= 5.0)575 for ductile/'special' RC moment frames. The range of R values can 576 be considered to be narrow, indicating a consistent storey-level 577 performance for all frames (note that the failure is governed by 578 an interstorey drift ratio based limit state for all frames). The taller 579 frames among the four studied show lower R values. Component-580 wise, the shorter frames (two-storey and four-storey) have more 581 overstrength and  $R_s$ , but slightly less ductility and  $R_{\mu}$  compared 582 to the taller frames. 583

584

# 7.2. Computation of R for PL2

It is observed that for the study frames, where maximum the 585 design base shear is around 6.0% of the seismic weight, the inter-586 storey drift ratio based limits become the same for both the 'Struc-587 tural Stability' and 'Life Safety' performance levels of ATC-40. 588 Therefore, the PL1 limits adopted in this work may be argued to 589 be conservative, and not representing the 'ultimate' limit state 590 for these structures [30]. Considering this, the actual plastic rota-591 tion capacities of member sections - based on their cross-sectional 592 properties including reinforcements - are considered for defining 593 the 'ultimate' limit state in PL2. Thus, PL2 remains a member level 594 limit state while in PL1 both structure and member level failures 595 are considered. 596

#### Table 11

Pushover parameters for PL1, considering  $P-\Delta$  effects.

| Frame     | $V_d$ (kN) | $V_u$ (kN) | $\Delta_y(\mathbf{m})$ | $\Delta_u(m)$ | Limiting parameter | $\mu = \varDelta_u / \varDelta_y$ | $\Omega = V_u/V_d$ |
|-----------|------------|------------|------------------------|---------------|--------------------|-----------------------------------|--------------------|
| 2-Storey  | 279        | 720        | 0.0957                 | 0.182         | IDR, storey 1      | 1.90                              | 2.58               |
| 4-Storey  | 371        | 938        | 0.160                  | 0.310         | IDR, storey 1      | 1.93                              | 2.53               |
| 8-Storey  | 416        | 928        | 0.231                  | 0.460         | IDR, storey 2      | 1.99                              | 2.23               |
| 12-Storey | 451        | 949        | 0.314                  | 0.617         | IDR, storey 1      | 1.97                              | 2.11               |

IDR stands for interstorey drift ratio.

Table 12 Components of R based on PL1 and PL2 (considering  $P-\Delta$  effects).

| Frame     | Based on PL1   |           |       | Based on PL2 |                |           |       |      |
|-----------|----------------|-----------|-------|--------------|----------------|-----------|-------|------|
|           | R <sub>s</sub> | $R_{\mu}$ | $R_R$ | R            | R <sub>s</sub> | $R_{\mu}$ | $R_R$ | R    |
| 2-Storey  | 2.58           | 1.92      | 1.00  | 4.96         | 2.58           | 3.20      | 1.00  | 8.48 |
| 4-Storey  | 2.53           | 1.97      | 1.00  | 4.97         | 2.53           | 2.59      | 1.00  | 6.54 |
| 8-Storey  | 2.23           | 2.04      | 1.00  | 4.56         | 2.23           | 2.45      | 1.00  | 5.46 |
| 12-Storey | 2.11           | 2.01      | 1.00  | 4.23         | 2.11           | 3.37      | 1.00  | 7.09 |

597 The plastic rotation capacities of beam and column sections are 598 obtained on the basis of their moment-curvature characteristics as described in Section 5.2. Similar to PL1, the nonlinear static push-599 over analyses are performed on the four frames and all the neces-600 sary responses are monitored till the plastic rotation capacity in 601 602 any member is reached. Figs. 9-12 also mark on the pushover plots when PL2 is reached, for both with and without P-4 effects. Table 603 604 13 provides the important parameters obtained from these push-605 over plots, including the ductility and the overstrength. Similar 606 to Table 11, this table marks the location where the limiting plastic 607 rotation for PL2 is reached first.

608 The pushover plots clearly show that, for all frames, PL2 is 609 reached after PL1 (that is, for a larger roof displacement). Based on the pushover plots (and their bilinearisation),  $V_{\mu}$  values come 610 611 out to be the same as those for PL1. Since  $V_d$  values do not change, 612  $\Omega$  values are also the same as in PL1. There are very minor varia-613 tions from PL1 values for  $\Delta_v$  values.  $\Delta_u$  values for PL2, as men-614 tioned earlier, are larger than corresponding PL1 values. and so 615 are the ductility values for each frame. Among the various compo-616 nents of R (presented in Table 12),  $R_s$  remains the same as in PL1, while  $R_{\mu}$  values come out to be higher, which finally results in 617 618 higher R factors overall. For PL2, R ranges from 5.46 to 8.48. This increased variation in R signifies that the four designs are not very 619 620 consistent in terms of a member rotation based performance level.

7.3. Effects of not adhering to the strong-column-weak-beam criterion 621

It may be noted that the strong-column-weak-beam (SCWB) 622 623 design is a desirable but not mandatory requirement as far as the Indian seismic design standard is concerned. Therefore, it is possi-624 ble to meet all the (Indian) codal requirements for these four de-625 signs without looking at the 'flexural' SCWB criterion defined in 626 terms of relative moment capacities of members at each beam-col-627 umn joint. Alternative designs for the four study buildings are thus 628 obtained without looking at the SCWB criterion. The section details 629 630 for these alternative designs are provided in Table 14. It is observed that in most of these cases, the design requirement for elements considering all the code specified load combinations for gravity and seismic loads - requires member sizes in such a way that the SCWB criterion is automatically satisfied. However in few other cases, particularly in the upper stories, the design requirements are met with a weak-column-strong-beam configuration. This happens for the internal columns in the upper stories of the four-, eight-, and 12-storey frames. The response reduction factor for these designs are computed for both PL1 and PL2, and are presented in Table 15. For PL1, values of *R* remain the same as those for the original designs considering the SCWB criterion, which signifies that the SCWB and non-SCWB designs do not differ from a maximum interstorey drift demand perspective. Even for PL2, the values of R are not significantly affected by the SCWB to non-SCWB shift in the design.

#### 7.4. Sensitivity to the fundamental period used in computing R

An accurate estimation of the fundamental period of vibration  $(T_1)$  of a structure is important in the determination of its R factor. The computation of the design base shear depends on  $T_1$ .  $T_1$  also determines the ductility factor  $(R_{\mu})$  based on the displacement ductility,  $\mu$ . Standard design practices typically use code-recommended empirical equations for estimating the design base shear. The same practice is followed here in calculating  $V_d$  for the four study frames. However, to obtain  $R_{\mu}$  from the  $R_{\mu}^{-}T$  relations developed by Krawinkler and Nassar [12],  $T_1$  is based on an eigensolution of the structural model used in DRAIN-2DX. The accuracy of the estimation based on eigensolution depends on how close the structural model is to the actual structure, particularly in modelling the mass and stiffness properties. Considering the standard modelling practices adopted in this work,  $T_1$  based on the eigensolution can be assumed to be sufficiently accurate for computing R. In this section, we check the effects of using  $T_1$  based on the coderecommended empirical equation in the  $R-\mu-T$  relations. IS 1893 [3] suggests an approximate formula for estimating  $T_1$  of a RC moment framed building without brick infill panels:

$$T_1 = 0.075h^{0.75} \tag{11}$$

where  $T_1$  is measured in seconds and h is the height of the building in metres. Other seismic design standards also suggest similar empirical equations for  $T_1$ , and these equations typically give a 'conservative' value, such that  $V_d$  is estimated on the higher side.

Fundamental time periods for the four frames based on this equation, along with the ones based on eigensolution, are provided in Table 16. The code-based  $T_1$  values are in the range of 50.0–

| Table 13 |            |          |             |             |
|----------|------------|----------|-------------|-------------|
| Pushover | parameters | for PL2, | considering | <b>P</b> −∠ |

| Pushover paramete | Pushover parameters for PL2, considering P- $\Delta$ effects. |            |                        |                        |                            |                             |                    |  |  |  |  |  |
|-------------------|---|------------|------------------------|------------------------|----------------------------|-----------------------------|--------------------|--|--|--|--|--|
| Frame             | $V_d$ (kN)  | $V_u$ (kN) | $\Delta_y(\mathbf{m})$ | $\Delta_u(\mathbf{m})$ | Limiting parameter         | $\mu = \Delta_u / \Delta_y$ | $\Omega = V_u/V_d$ |  |  |  |  |  |
| 2-Storey          | 279   | 720        | 0.104                  | 0.332                  | $\theta_p$ , ground column | 3.20                        | 2.58               |  |  |  |  |  |
| 4-Storey          | 371   | 938        | 0.164                  | 0.409                  | $\theta_p$ , storey 1 col. | 2.50                        | 2.53               |  |  |  |  |  |
| 8-Storey          | 416   | 928        | 0.237                  | 0.560                  | $\theta_p$ , storey 1 col. | 2.36                        | 2.23               |  |  |  |  |  |
| 12-Storey         | 451   | 949        | 0.336                  | 1.07                   | $\theta_p$ , storey 1 col. | 3.18                        | 2.11               |  |  |  |  |  |

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#### Table 14

RC section details for the study frames (without the SCWB design criterion).

| Frame     | Members          | Floors | Width (mm) | Depth (mm) | Reinforcement details  |
|-----------|------------------|--------|------------|------------|--|
| 2         | Beams            | 1-2    | 250        | 500        | $[3 - 25\Phi + 2 - 20\Phi]$ (top) + $[2 - 25\Phi + 1 - 20\Phi]$ (bottom) |
| 2-storey  | Interior columns | 1-2    | 450        | 450        | $8 - 25\Phi$ (uniformly distributed)                                     |
|           | Exterior columns | 1-2    | 450        | 430        | $8 - 25\Phi$ (uniformity distributed)                                    |
|           | Beams            | 1-4    | 300        | 600        | $6 - 25\Phi$ (top) + $3 - 25\Phi$ (bottom)                               |
| 4-storey  | Interior columns | 1-4    | 500        | 500        | $4 - 28\Phi + 4 - 25\Phi$ (uniformly distributed)                        |
|           | Exterior columns | 1-4    | 500        | 500        | $12-25\Phi$ (uniformly distributed)                                      |
|           | Beams            | 1-4    | 300        | 600        | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                              |
|           | Interior columns | 1-4    | 600        | 600        | $12 - 25\Phi$ (uniformly distributed)                                    |
| 8-storey  | Exterior columns | 1-4    | 600        | 600        | $12 - 25\Phi$ (uniformly distributed)                                    |
|           | Beams            | 5-8    | 300        | 600        | $6 - 25\Phi$ (top) + $3 - 25\Phi$ (bottom)                               |
|           | Interior columns | 5-8    | 500        | 500        | $8-25\Phi$ (uniformly distributed)                                       |
|           | Exterior columns | 5-8    | 500        | 500        | $12 - 25\Phi$ (uniformly distributed)                                    |
|           | Beams            | 1-4    | 300        | 650        | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                              |
|           | Interior columns | 1-4    | 750        | 750        | $12 - 25\Phi$ (uniformly distributed)                                    |
|           | Exterior columns | 1-4    | 750        | 750        | $12 - 25\Phi$ (uniformly distributed)                                    |
|           | Beams            | 5-8    | 300        | 600        | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                              |
| 12-storey | Interior columns | 5-8    | 600        | 600        | $12 - 25\Phi$ (uniformly distributed)                                    |
|           | Exterior columns | 5-8    | 600        | 600        | $12-25\Phi$ (uniformly distributed)                                      |
|           | Beams            | 8-12   | 250        | 550        | $6 - 25\Phi$ (top) + 3 - 25 $\Phi$ (bottom)                              |
|           | Interior columns | 8-12   | 500        | 500        | $8 - 25\Phi$ (uniformly distributed)                                     |
|           | Exterior columns | 8-12   | 500        | 500        | $12 - 25\Phi$ (uniformly distributed)                                    |

 $\Phi$  is the diameter of a rebar.

#### Table 15

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Components of R, without the SCWB design criterion.

| Frame     | Based on PL1 |           |       |      | Based on PL2 |           |       |      |
|-----------|--------------|-----------|-------|------|--------------|-----------|-------|------|
|           | Rs           | $R_{\mu}$ | $R_R$ | R    | Rs           | $R_{\mu}$ | $R_R$ | R    |
| 2-Storey  | 2.58         | 1.92      | 1.00  | 4.96 | 2.58         | 3.20      | 1.00  | 8.48 |
| 4-Storey  | 2.33         | 2.13      | 1.00  | 4.97 | 2.33         | 2.79      | 1.00  | 6.52 |
| 8-Storey  | 2.20         | 2.05      | 1.00  | 4.53 | 2.20         | 2.67      | 1.00  | 5.88 |
| 12-Storey | 2.11         | 2.01      | 1.00  | 4.23 | 2.11         | 3.52      | 1.00  | 7.41 |

676 60.0% of the  $T_1$  based on the eigensolution. Table 16 also provides the values of *R* (for both PL1 and PL2) based on the code-based  $T_1$ 677 678 values. The effect of the reduction in  $T_1$  on R ( $R_{\mu}$ , to be more spe-679 cific) is observed only for the two- and four-storey frames. For 680 these two frames  $R_{\mu}$  changes, while there is (almost) no change in  $R_{\mu}$  for the other two frames. Fig. 2 explains this phenomenon. 681 For the two- and four-storey frames, the reduction in R is more 682 683 in PL2 than in PL1. In this context, it should also be mentioned that there is an elongation of  $T_1$  when the structure goes into its inelas-684 685 tic behaviour. This elongation may cause an increase in  $R_{\mu}$ , only if the elastic  $T_1$  was in the 'constant acceleration' range (typically, be-686 low 0.5-0.7 s). 687

# 688 7.5. Effects of not including $P_{-1}$ effects in analyses

The nonlinear static pushover analyses, used so far for obtaining values of *R* for two performance levels, included  $P_{-2}$  effects in order to reflect the structural behaviour as accurately as possible. As an academic exercise, we check here if the inclusion or exclusion of

these effects is important at the selected performance levels (PL1 693 and PL2) for the four study frame. Pushover plots for these frames 694 without the global P-1 effects are shown in Figs. 9–12 along with 695 'with  $P-\Delta$ ' plots, for an easy comparison. As expected, the 'without 696  $P-\Delta'$  plots show a monotonically non-decreasing (in terms of the 697 base shear) curve, unlike the 'with  $P_{-\Delta}$ ' plots which show a down-698 ward curve after attaining a maximum base shear ( $V_u$ ). Table 17 699 presents the results of these 'without  $P-\Delta$ ' analyses in terms of R 700 and its components. For PL1, there is an increase in  $R_s$  and the final 701 R values range between 4.86 and 5.50, which are around the IS 702 1893 specified value of 5.0. However for PL2, there is a significant 703 increase in  $R_{\mu}$ , along with some increase in  $R_s$ . This causes a very 704 visible rise in R values for all frames, to the range of 8.79-10.9. 705 The effects  $P_{-1}\Delta$  are more significant on  $\theta_p$  at the member Tevel than 706 on interstorey drift ratios, which causes a significant difference in 707  $R_{\mu}$  values between with and without  $P_{\perp} \Delta$  analyses. 708

#### 7.6. Effects of the lateral load distribution pattern used in NSPA

Values of *R* computed so far are based on pushover analyses710considering the quadratic lateral distribution pattern suggested711in IS 1893 (Eq. (10)). It should be worthwhile to check if these value change (and if they do, to what extent they change) if we considered a different lateral load distribution in the NSPA. ASCE7 [1]714suggested a distribution based on the fundamental vibration period ( $T_1$ ):716

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$$Q_i = V_d \frac{W_i h_i^k}{\sum\limits_{i=1}^n W_i h_i^k}$$
(12)

| Table 16                 |                         |                |        |
|--------------------------|-------------------------|----------------|--------|
| Components of R based of | on the code-recommended | fundamental pe | eriod. |

| Frame     | Fundament | al period, $T_1$ (s) | Based on | Based on PL1 |       |      |       | Based on PL2 |       |      |  |
|-----------|-----------|----------------------|----------|--------------|-------|------|-------|--------------|-------|------|--|
|           | Code      | Eigensolution        | Rs       | $R_{\mu}$    | $R_R$ | R    | $R_s$ | $R_{\mu}$    | $R_R$ | R    |  |
| 2-Storey  | 0.453     | 0.884                | 2.58     | 1.83         | 1.00  | 4.73 | 2.58  | 2.89         | 1.00  | 7.46 |  |
| 4-Storey  | 0.683     | 1.16                 | 2.53     | 1.92         | 1.00  | 4.86 | 2.53  | 2.48         | 1.00  | 6.28 |  |
| 8-Storey  | 1.08      | 1.97                 | 2.23     | 2.03         | 1.00  | 4.53 | 2.23  | 2.42         | 1.00  | 5.41 |  |
| 12-Storey | 1.43      | 2.60                 | 2.11     | 2.01         | 1.00  | 4.24 | 2.11  | 3.37         | 1.00  | 7.09 |  |

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Table 17

Components of *R*, without the  $P-\Delta$  effects.

| Frame     | Based on PL1 |           |       |      | Based on PL2 |           |       |      |
|-----------|--------------|-----------|-------|------|--------------|-----------|-------|------|
|           | $R_s$        | $R_{\mu}$ | $R_R$ | R    | $R_s$        | $R_{\mu}$ | $R_R$ | R    |
| 2-Storey  | 2.79         | 1.97      | 1.00  | 5.50 | 2.82         | 3.86      | 1.00  | 10.9 |
| 4-Storey  | 2.76         | 1.93      | 1.00  | 5.32 | 2.77         | 3.17      | 1.00  | 8.79 |
| 8-Storey  | 2.55         | 1.91      | 1.00  | 4.86 | 2.60         | 3.55      | 1.00  | 9.22 |
| 12-Storey | 2.46         | 1.98      | 1.00  | 4.88 | 2.62         | 3.77      | 1.00  | 9.89 |

where *k* is an exponent related to  $T_1$ : for  $T_1 \leq 0.5$  s, k = 1.0; for  $T_1 \geq 2.5$  s, k = 2.0; and *k* is linearly interpolated between these values for 0.5 s  $< T_1 < 2.5$  s. This is also recommended by design standards such as the International Building Code (IBC), USA. Some other design standards and guidelines, such as EC8 or ATC-40, suggested a distribution based on the fundamental mode shape ( $\phi_1$ ):

$$Q_i = V_d \frac{W_i \phi_{1i}}{\sum_{i=1}^n W_i \phi_{1i}}$$
(13)

729 where  $\phi_{1i}$  is the *i*th floor element in  $\phi_1$ . The lateral load distribution 730 determines the storey shear for each frame. For example, the distri-731 bution of storey shear (normalised to  $V_d = 1.0$ ) for different lateral 732 load distributions are shown in Fig. 13 for the eight-storey frame.

Values of R and its components considering lateral load distribu-733 tions based on ASCE7 and the fundamental mode shape are shown 734 in Tables 18 and 19, respectively. Other considerations in these 735 736 computations remain the same as in Sections 7.1 and 7.2. As shown 737 in the sample pushover curves for the eight-storey frame (Fig. 14), 738 the ultimate performance points are slightly affected by a change in 739 the distribution of Q<sub>i</sub> adopted in the NSPA. For PL1, the R values in-740 crease (from those based on the IS 1893 distribution) to the range of 741 4.56–5.27 for the ASCE7 distribution and to 4.70–5.50 for the  $\phi_1$ -



**Fig. 13.** Typical storey shear pattern of the eight-storey frame for different lateral load distributions.

#### Table 18

Components of R considering a lateral load distribution as per ASCE7.

| Frame   | Based on PL1                 |                              |                              |                              | Based on PL2                 |                              |                              |                              |
|---|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|
|   | Rs                           | $R_{\mu}$                    | $R_R$                        | R                            | R <sub>s</sub>               | $R_{\mu}$                    | $R_R$                        | R                            |
| 2-Storey<br>4-Storey<br>8-Storey<br>12-Storey | 2.76<br>2.63<br>2.34<br>2.20 | 1.91<br>1.73<br>2.10<br>2.11 | 1.00<br>1.00<br>1.00<br>1.00 | 5.27<br>4.56<br>4.91<br>4.64 | 2.76<br>2.63<br>2.34<br>2.20 | 2.88<br>2.35<br>2.53<br>3.00 | 1.00<br>1.00<br>1.00<br>1.00 | 7.94<br>6.18<br>5.92<br>6.00 |

#### Table 19

Components of R considering a lateral load distribution based on the fundamental mode shape.

| Frame   | Based on PL1                 |                              |                              |                              | Based on PL2                 |                              |                              |                              |
|---|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|
|   | $R_s$                        | $R_{\mu}$                    | $R_R$                        | R                            | $R_s$                        | $R_{\mu}$                    | $R_R$                        | R                            |
| 2-Storey<br>4-Storey<br>8-Storey<br>12-Storey | 2.70<br>2.64<br>2.39<br>2.26 | 2.03<br>2.01<br>2.05<br>2.08 | 1.00<br>1.00<br>1.00<br>1.00 | 5.50<br>5.31<br>4.90<br>4.70 | 2.70<br>2.64<br>2.39<br>2.26 | 3.02<br>2.32<br>2.51<br>2.83 | 1.00<br>1.00<br>1.00<br>1.00 | 8.16<br>6.14<br>5.98<br>6.39 |



Fig. 14. Pushover curves for the eight-storey frame for different lateral load distributions.

based distribution. For the  $\phi_1$ -based distribution, both the ductility and strength factors increase, while it is only the strength factor increasing for the ASCE7 distribution. Similar changes are observed for PL2, both for *R* and its components, where *R* increases (except for the two-storey frame) to the ranges of 5.92–7.94 and 5.98–8.16, respectively.

# 8. Concluding remarks

A detailed study has been conducted to check the validity of the response reduction factor (R) value recommended in IS 1893 for 'ductile'/'special' RC moment resisting frames. The work presented here has considered four RC moment framed buildings, with fundamental vibration periods covering a large spectrum, located in zone IV and designed and detailed following the Indian standard guidelines IS 1893 and IS 13920. The focus has been in the following areas: a component-wise calculation of the factor R; consideration of realistic performance-based limit states at both structure and member levels; detailed modelling of the inelastic moment-curvature behaviour, P-M interaction, and plastic rotation capacity; and consideration of realistic design practices.

The major conclusions of the research presented here are

- Based on *Performance Limit 1* (ATC-40 limits on interstorey drift ratio and member rotation capacity), the Indian standard overestimates the *R* factor, which leads to the potentially dangerous underestimation of the design base shear.
- The actual value of *R* in real life designs is expected to be even lower than what is computed here, because of various reasons, such as, irregularity in dimensions leading to minor to moderate torsional effects, lack of quality control and poor workmanship during the construction, not following the ductile detailing requirements exactly as per the guidelines, etc.

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- Based on *Performance Limit 2* (member rotation limits based on section dimensions and actual reinforcements), the IS 1893 recommendation is on the conservative side. It should however be noted that this limit does not include any structure level behaviour such as interstorey drift.
  - The strong-column-weak-beam criterion in design does not make any major difference in terms of *R*.
  - An accurate estimation of the fundamental period  $(T_1)$  is necessary for estimating a realistic *R* of a structure, specifically if  $T_1$  is in the constant  $S_a$  zone of the design spectrum.
  - *R* (for PL1) comes to be close to the IS 1893 recommended value if  $P_{\perp} \Delta$  effects are not considered. So, *R* = 5.0 may be safe for a design where  $P_{\perp} \Delta$  effects are actually negligible at the ultimate state.
  - The IS 1893 and the ASCE7 lateral load distributions give *R* almost in the same range. However, a load distribution based on the fundamental mode shape estimates *R* in a range of higher values.

The conclusions of the present study are limited by the facts that only a single plan configuration (without plan-asymmetry) in one single seismic zone has been considered. In addition, the structural behaviour is not validated by any nonlinear response-/ time-history analysis. The different parameters used in the work presented have been considered to be deterministic, although in reality their statistical variations are significant enough requiring a reliability-based framework for this study.

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