

Toll Operation

Lecture Notes in Transportation Systems Engineering

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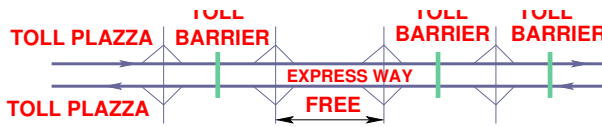


Figure 1: Open Toll System

1 Introduction

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Toll tax is collected to recover the total capital outlay which includes the cost of construction, repairs, maintenance, expenses on toll operation and interest on the outlay. The new facility thus constructed should provide reduced travel time and increased level of service. In India most of the highway projects are given on PPP basis, i.e. Public Private Partnership. In this the private organization finances and constructs the facility and recovers the capital from the users in the form of toll tax. This tax is collected for a reasonable period of time after which the facility is surrendered to the public. Of late, toll tax is being levied on parking of vehicles in the urban centers in a move to decongest the streets and reduce the pollution levels. This concept is known as Congestion Pricing.

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1.1 Types of Toll Collection

There are two types of toll collection systems available. These are: (i) Open Toll System, and (ii) Closed Toll System.

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1.1.1 Open toll System

In an open toll system, not all patrons are charged a toll. In such a system, the toll plaza is generally located at the edge of the urban area, where a majority of long distance travelers are committed to the facility, with a minimum likelihood of switching to the parallel free route, or at the busiest section of the toll way [2]. Patrons are identified by their category and pay a fixed toll for it. The local traffic around the plaza either gets rebate or can use a service lane. The general layout of an open toll collecting system is highlighted in Fig. 1.

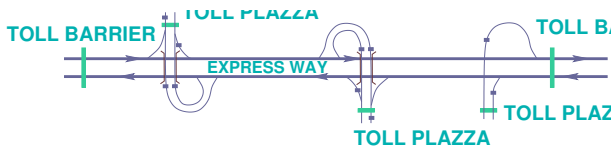


Figure 2: Closed Toll System

1.1.2 Closed toll System

In a closed toll system, patrons pay the toll based on miles of travel on the facility and category of vehicle. There are no free-rides. In a closed toll system, plazas are located at all the entry and exit points, with the patron receiving a ticket upon entering the system. Upon exiting, patron surrenders the ticket to the collector and is charged a prescribed fee based on category of vehicle and distance travelled [2]. It has just two stops for the vehicles whereas open system can have multiple stops. But closed system is expensive to construct than open system. The general layout of an open toll collecting system is highlighted in Fig. 2.

1.2 Methods of Toll Collection

There are three methods of toll collection available. These are: (i) Manual, (ii) Automatic, and (ii) Electronic.

1.2.1 Manual Toll Collection

Manual toll collection is most widely used collection method in India. It requires a toll collector or attendant. Based on the vehicle classification, cash toll is received by the collector. The collector, who also dispenses change, may accept and sell scrip, tickets, coupons, making an entry of the vehicle in the system and issuing receipt to the patron [2]. Due to manual intervention, the processing time is highest.

1.2.2 Automatic Toll Collection

Automatic toll collection is based on the use of Automated Coin Machine (ACM). These accept both coins and tokens issued by the operating agency. Depending on the toll

rate, the use of automated coin or token collection instead of manual collection reduces transaction and processing time as well as the operating cost.

1.2.3 Electronic Toll Collection

Electronic Toll Collection (ETC) is a system that automatically identifies a vehicle equipped with a valid encoded data tag or transponder as it moves through a toll lane or check-point. The ETC system then posts a debit or charge to a patron's account, without the patron having to stop to pay the toll. ETC increases the lane throughput because vehicles need not stop to pay the toll.

1.3 Terminology

Some of the basic terms that will be used in the chapters to come have been discussed in this section. Following are the terms and their definitions:

1. **Throughput:** It is the number of vehicles passing through the toll plaza over a short period of time, usually 1 hour.
2. **Demand:** It is the sum of throughput and the number of vehicles queued up at the toll plaza during 1 hour.
3. **Processing Time:** It is the difference between the time a vehicle leaves and the time when it enters the toll area. The entry time is taken from the moment a vehicle stops in the queue.
4. **Queueing Area:** It is the area of the toll plaza where the number of lanes of incoming vehicles increase from the number of lanes on highway to the number of tollbooths. The vehicles queue up in this area to make the toll payment. Fig. 3 shows the location of queueing area in a toll plaza.
5. **Merging Area:** It is the area of the toll plaza where the number of lanes of outgoing vehicles decrease from the number of tollbooths to the number of lanes on highway. The vehicles have to merge with other vehicles in this area before the highway comes to its normal width. Fig. 3 shows the location of merging area in a toll plaza.

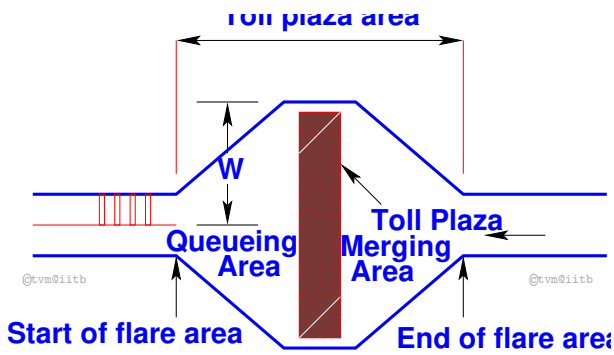


Figure 3: Toll Plaza Geometry

6. **Optimal Toll Plaza Configuration:** It is the one which minimizes the expected time a driver must spend while travelling through the system.

2 Optimum Number of Toll Booths

The entire toll plaza area can be divided into two areas namely queueing and the merging area. The vehicles line up to pay the toll in the queueing area. The vehicles wait for their turn to pay the toll at the toll booth. The delay is called as the queueing delay. Similarly, once the vehicle crosses the toll booth, the number of lanes reduces from number of tollbooths to the original width of the highway. A vehicle travelling in a lane has to wait or slow down to allow another vehicle in the adjacent lane to pass. These kind of delays are termed as merging delays. We will apply Queueing Theory to ascertain the delays in both the areas. Keeping the total delay time to be minimum, we find the optimal number of tollbooths for the system. The time wasted at the tollbooth (W_A) is given by the equation. 1:

$$W_a = \frac{1}{\mu_a - \phi/T} \text{ sec/veh} \quad (1)$$

where, μ_a = Service rate at a tollbooth (veh/hr), ϕ = Total traffic flow (veh/hr), T = Number of tollbooths

Similarly, the time wasted at merging area is calculated using the following logic. If

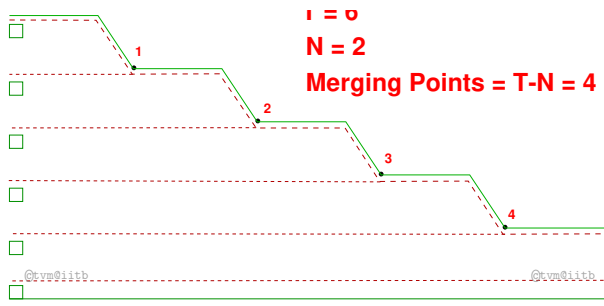


Figure 4: Merging points and conflicting lanes

there are T tollbooths which are finally merged into N lanes of highway then the number of merging points are given by $(T - N)$ (see Fig. 4). From Fig. 4 we can see that in a toll plaza with a side merging layout which has T tollbooths, the first merging point takes a stream coming from 2 tollbooths, and the second merging point would take a stream from 3. By Little's theorem, the average waiting time in the system $t_{sys}(\lambda)$ is given by the equation. 2:

$$t_{sys}(\lambda) = \frac{L(\lambda)}{\lambda} = \frac{1}{\mu_B - \lambda} + \frac{\mu_B - \mu_0}{\lambda(\mu_B - \mu_0) + \mu_0\mu_B} \quad (2)$$

The average wasted time of a driver at a merging point is the difference between t_{sys} and the time he or she would spend on a normal lane. The expected time a driver spends when no merging happens is $1/\mu_0$. Hence, the average wasted time is given by the equation. 3.

$$t_{diff}(\lambda) = t_{sys}(\lambda) - \frac{1}{\mu_0} = \frac{1}{\mu_B - \lambda} + \frac{\mu_B - \mu_0}{\lambda(\mu_B - \mu_0) + \mu_0\mu_B} - \frac{1}{\mu_0} \quad (3)$$

where, μ_B = Service rate when merging of vehicles takes place (veh/hr), μ_0 = Service rate when no merging of vehicles takes place (veh/hr), λ = Vehicle arrival rate = $(k/T) \times \phi$ (veh/hr), k = No. of conflicting lanes at a merging point. k has a range between $[2, T - N + 1]$

The above formula gives the average wasted time of a driver at each merging point. The overall wasted time is the weighted sum of all the wasted time at each merging point, where the corresponding weight is the probability for a driver to reach that point.

The overall wasted time (W_B) can be calculated using the equation. 4.

$$W_B = \sum_{i=1}^{T-N} \frac{i+1}{T} \times t_{diff} \left(\frac{i+1}{T} \times \phi \right) \text{ sec/veh} \quad (4)$$

As per the optimal toll plaza configuration, we need to keep the total delay time as minimum [4]. The Total Wasted Time (W_{total}) for the vehicle (Tollbooth + Merging) is given by the equation. 5:

$$W_{total} = W_A + W_B = \frac{1}{\mu_A - \phi/T} + \sum_{i=1}^{T-N} \frac{i+1}{T} \times t_{diff} \left(\frac{i+1}{T} \times \phi \right) \quad (5)$$

2.0.1 Numerical example

Calculate the Total delay time in toll plaza if the total no of tolls are 3 on a single-lane highway. The total traffic flow on the highway is 800 veh/hr. Assume the following data: Service rate of Tollbooth = 400 veh/hr; Service rate when merging of vehicles takes place = 1500 veh/hr; Service rate when no merging of vehicles takes place = 2500 veh/hr

Solution: The following data has been given to us in the problem: $N=1$ lane; $\phi = 800$ veh/hr; $\mu_A = 400$ veh/hr; $\mu_B = 1500$ veh/hr; $\mu_0 = 2500$ veh/hr. Our aim is to determine the total delay time in toll plaza. From eqn above ; $W_A = \frac{1}{(400 - \frac{800}{3})} = 0.0075$ hr/veh = 27 sec/veh. It means that the wasted time at the tollbooth is 27 sec/veh. Now we move on to find the overall wasted time in the merging area (WB). To find that, first we need to find the wasted time at each merging point which can be calculated using the equation. Now, eqn uses a term k in it which signifies the number of conflicting lanes at each merging point. k ranges between [2, T-N+1]. Therefore in this case (T=3) k lies between [2, 4-1+1], i.e. [2,3] When K=2: Hence, λ at first merging point = $(\frac{2}{3}) \times 800 = 533.3 \text{ veh/hr}$. From eqn above, for ($\lambda = 533.33$)

$$T_{diff} = \frac{1}{(1500 - 2 \times \frac{800}{3})} + \frac{(1500 - 2500)}{[2 \times \frac{800}{3} (1500 - 2500) + 1500 \times 2500]} - \frac{1}{2500} = 1.166 \text{ sec.}$$

WB for the 1st merging point = $(\frac{2}{3}) \times 1.166 = 0.777 \text{ sec}$ When K=3: $(\frac{3}{3})$

$$T_{diff} = \frac{1}{(1500 - 3 \times \frac{800}{3})} + \frac{(1500 - 2500)}{3} \times \frac{800}{3} (1500 - 2500) + 1500 \times 1500 - \frac{1}{2500}$$

tsys = 2.48 sec. WB for the 2st merging point = $(\frac{3}{3}) \times 2.48 = 2.48 \text{ sec}$. Total WB = 0.777 + 2.48

WB = 3.257 sec. Wtotal = WA + WB = 27.0 + 3.257. Total delay time Wtotal = 30.257 sec.

2.0.2 Numerical example

Calculate the optimum number of tollbooths to be installed on a toll plaza, proposed to be built on a single-lane highway. The total traffic flow on the highway is 900 veh/hr. Assume the following data: Service rate of Tollbooth = 350 veh/hr; Service rate when merging of vehicles takes place = 1184.9 veh/hr; and Service rate when no merging of vehicles takes place = 3017.1 veh/hr.

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Solution: The following data has been given to us in the problem: $N=1$ lane; $\phi = 900$ veh/hr; $\mu_A = 350$ veh/hr; $\mu_B = 1184.9$ veh/hr; $\mu_0 = 3017.1$ veh/hr. Our aim should be to determine the total vehicle delays for different values of tollbooths (T). The value of T corresponding to which the delay time is minimum is the optimal condition. Let us initially start with $T=4$; From equation. 1; $W_A = 1/(350 - 900/4) = 0.008$ hr/veh = 28.8 sec/veh. It means that the wasted time at the tollbooth is 28.8 sec/veh. Now we move on to find the overall wasted time in the merging area (W_B). To find that, first we need to find the wasted time at each merging point which can be calculated using the equation. 3. Now, equation. 3 uses a term k in it which signifies the number of conflicting lanes at each merging point. It can be seen from figure 4 that k ranges between $[2, T - N + 1]$. Therefore in this case ($T=4$) k lies between $[2, 4-1+1]$, i.e. $[2, 4]$. Hence, λ at first merging point = $(2/4) * 900 = 450$ veh/hr. From equation. 3, ($\lambda = 450$)

$$T_{diff} = 1/(1184.9 - 2 \times 900/4) + (1184.9 - 3017.1)/[2 \times 900/4(1184.9 - 3017.1) + 1184.9 \times 3017.1] - 1/3017.1 = 1.307 \text{ sec.}$$

Similarly, λ at second merging point = $(3/4) * 900 = 675$ veh/hr and λ at third merging point = $(4/4) * 900 = 900$ veh/hr. Using equation. 3, the values of t_{diff} can be found out at second and third merging points. t_{diff} at second merging point, $t_{diff} (\lambda=675) = 3.046$ sec. t_{diff} at third merging point, $t_{diff} (\lambda=900) = 8.018$ sec. Now the overall wasted time in merging (W_B) is given by the equation. 4 which is the product of the weighted mean of the merging point with the t_{diff} values. Hence, $W_B = (2/4) * 1.307 + (3/4) * 3.046 + (4/4) * 8.018 = 6.176$ sec. Now, W_{total} can be calculated from equation. 5 which is sum of W_A and W_B . $W_{total} = 28.8 + 6.176 = 34.976$ sec. So, for the case of $T=4$, the total wasted time is 34.976 secs. Following the same procedure to calculate W_{total} for different values of T . For faster calculation purposes, we can use Microsoft Excel to compute the values of W_A , t_{diff} , W_B and W_{total} . Following are the wasted times for different values of T . We can clearly see that the total delay is minimum for

Table 1: Total wasted time for different number of tollbooth

T	W_A	T_{sys}	W_B	W_{total}
4	28.8	12.371	6.176	34.976
6	18	16.403	13.839	31.839
8	15.15	20.436	16.805	31.955
10	13.846	24.476	19.815	33.661

the configuration $T=6$. Hence 6 tollbooths is the optimal solution for the given highway facility.

3 Toll Plaza Design Specifications

The Concessionaire shall provide required number of Toll Plazas for collection of toll as per the Concession Agreement. The fee collection system shall be speedy, efficient and user friendly. The design of the Toll Plazas should be such that they are aesthetically pleasing and efficient and the fee collection staff should be quick, courteous and adequately trained before deployment.

3.1 General Layout

Fig. 5 shows the general toll plaza geometry of a 2+2 lane toll plaza. Initially, the numbers of lanes become equal to the number of tollbooths, which is equal to three in Fig. 5, in the queueing area. After the vehicle crosses the tollbooth, the number of lanes merges back to the original width of the highway, i.e. two-lane. A lane for the extra wide and the exempted vehicles is provided at the left hand side of the highway. Some extra space is also maintained for the scope of future plaza expansion. The design specifications for the design of the flared portions are as listed below:

1. Lane width = 3.2 m in general and 4.1 m for oversize vehicles.
2. Median (a) Width = 1.8 m (b) Length = 50 m
3. Transition - 1 in 10 may be provided from two-lane section to the widened width at Toll Plaza on either side.

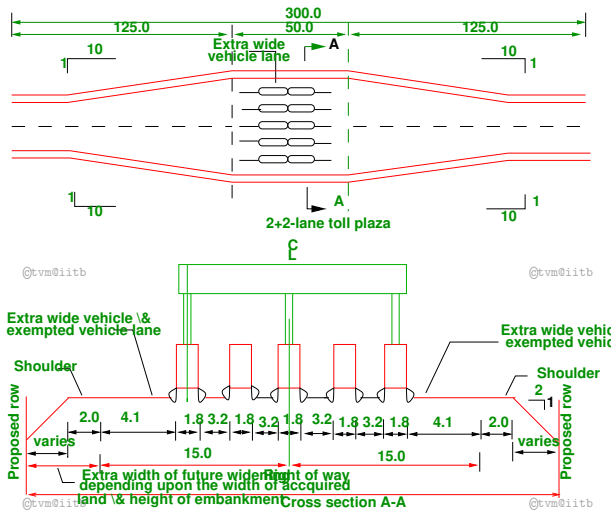


Figure 5: General Layout 2+2 lane Toll Plaza (Source: [3])

3.2 Number of Toll lanes

As discussed previously, tollbooths are erected to collect the tax from the road users. The number of tollbooths depends on the flow of vehicles on the facility. Following guidelines are generally followed while deciding the number of toll lanes in a toll plaza:

1. Peak Hour Factor: Percentage of vehicles travelling during the peak hour to the average daily traffic.
2. Number of toll lanes should be corresponding to the forecast traffic for at least 5 years.
3. Forecast traffic in terms of veh/day for all the tollable categories. Non-tollable vehicles (e.g. VIP vehicles, ambulances, etc) are exempted from the toll tax and flow through a separate lane.
4. If the queue becomes so long that the waiting time exceeds three minutes then the number of tollbooths need to be increased.

Table 2: Number of Semi Automatic Toll gates in each direction, Source: [3]

Forecast Traffic (in vehicles/day) total of both directions	Peak Hour Factor			
	6%	7%	8%	9%
Less than 7000	2	2	2	2
7000-12000	2	2	3	3
More than 12000	3	3	4	4

3.3 Toll Collection System

As discussed earlier, there are three methods of toll collection. Out of them, the manual method is the most time consuming whereas the delays are minimum for electronic system. Following measures are adopted for making the toll collection process a faster one.

1. A minimum semi-automatic system for toll collection should be adopted.
2. Collection of toll and recording of data would be made through electronic equipment.
3. Intercom facility shall be provided between booths and the office of the supervisors.
4. If any booth is closed for any reason, incoming traffic shall be guided into the adjoining working booth with the help of appropriate signs.

3.4 Tollbooth

A tollbooth is that location of the toll plaza where the tax is actually paid. This section lays emphasis on the procedures involved in the construction of a tollbooth.

1. Toll booths should be made from prefabricated materials or of brick masonry.
2. Toll booth should have space for seating for toll collector, computer system, printer and cash.

3.5 Traffic Signs

The traffic signs inform the users about the approaching toll plaza, prices for different categories. Some of the guidelines laid down are:

1. The driver should be reminded of a toll plaza at least 1km ahead of its existence. Another reminder should be given at 500m from the plaza.
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2. STOP sign should be marked on the pavement at the toll lanes.
3. Signs should be installed to inform the users about the toll price for different categories of vehicles.
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4. Electronic signs should be installed over the toll booths to display their operation status.
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3.6 Road Markings

The road markings help in channelizing the movement of vehicles in a toll plaza. These comprise of the diagonals, lanes and chevron markings. Following specifications are followed while doing the road markings.
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1. Single centre line is provided at the centre of the carriageway at toll gate to demarcate each service lane.
2. Diagonal markings for central traffic island and chevron marking sat side traffic island shall be provided to guide the approaching and separating traffic.

3.7 Lighting

Toll plaza lighting needs due consideration because user should be able to spot the existence of a toll plaza from a distance at night. The specifications for different types of lighting provided at a toll plaza are listed below:
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1. *Highway Lighting*: Lighting in 100m length on both sides of toll plaza shall be provided to enhance safety and to make drivers conscious of approaching a toll gate.

2. *Canopy Lighting*: Higher level of illumination shall be provided at the tollgate and toll booth locations.
3. *Interior lighting*: It should be 200-300 Lux as per IS:3646 (Part-II)
4. *High Mast Lighting*: IS:1944 (Part I & II) recommends 30 Lux of average illumination on road surface. 30m height of mast is considered suitable [3].

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4 Toll Pricing

Toll is a fee collected for the use of the road, bridge, tunnel, etc. to recover the total capital outlay which includes interest on outlay, cost of repairs, maintenance and also expenses on collection of toll. Hence the amount of toll should not exceed the benefits which the user receive while using the toll road. The benefits are due to savings in travel time, travel cost, increase in comfort and convenience. The toll structure should be fixed in such a way that investments and expenses are recovered within a reasonable period of time. The product of optimum toll rate and traffic volume finally determines the gross toll revenue.

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4.1 Factors Affecting Toll Rates

Two important factors determine the toll rates. They are:

1. **Traffic Volume**: Determining the traffic volume that will be using the facility is the most important factor. Success of any toll will virtually depend on the accurate estimation and forecasting of toll traffic and its composition.
2. **Willingness to pay**: Users will be willing to pay a realizable portion of their savings to use the improved facility.

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4.2 Conversion of Benefits into Monetary Terms

As mentioned above the toll rates should not be more than savings derived by the road user by using the facility. The savings will be perceived differently by people of different category and people using different modes. For public transport user, he/she is not concerned with vehicle operating cost. Instead, he/she is concerned with the fare to be

paid for the unit distance travelled. But for private mode, the user is concerned with the vehicle operating cost and travel time saved. Travel distance, travel time and toll are taken as deterrence measure. Maximum limit of toll as a deterrence is found, beyond which the suggested shortest path becomes uneconomical.

4.3 Optimum Toll Charges

Two factors are to be considered before fixing the optimum toll. They are:

1. Toll rate should be fixed in such a way that a vehicle owner should not shy away from using the facility.
2. The operator should get maximum toll revenue so that it can recover the total outlay cost in a reasonable period.

Toll rates of all the vehicles are obtained after including the maintenance cost and the interest on construction cost to the total outlay cost [1].

5 Conclusion

From the above discussions we can conclude that toll tax is a fee which is used for the use of a newly constructed facility to recoup the total capital outlay. The private organization builds, operates and then transfers the facility after a projected period of time. The Electronic Toll Collection (ETC) system is the most efficient method of toll collection with minimum delays. But due to its high installation cost it's not that prevalent in India. We can find the optimum number of tollbooths by applying queueing theory to ascertain the delays in both queueing and merging areas. The optimum number of tollbooths should minimize the overall delay time. The toll plaza design should be done in accordance with the Indian Standard Codes available. Toll prices are set in a way that they attract maximum number of users and the agency should be able to recover the cost within specified period of time.

Exercises

1. Not Available

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