

DEPARTMENT OF CIVIL ENGINEERING
CE-222 STRUCTURAL MECHANICS I
 Quiz-1 2/2/11

Problem 1

Draw the Axial Force, Shear Force, and Bending Moment Diagram for the frame shown in **Fig. 1**. Then, use this to sketch the Qualitative Deflected Shape.

Problem 2

The truss-beam bridge structure shown in **Fig. 2** comprises truss *AGHBJI* and three members *BCD*, *DF*, and *CE*. The truss is connected to member *BCD*. Members *BCD* and *CE* are connected by a pin/hinge at *C*. Members *BCD* and *DF* are connected by a pin/hinge at *D*. The load train shown passes over the bridge.

Find:

- (i) the maximum compressive force in member *EC*
- (ii) the maximum bending moment at *C* in member *BCD*

Figure 1

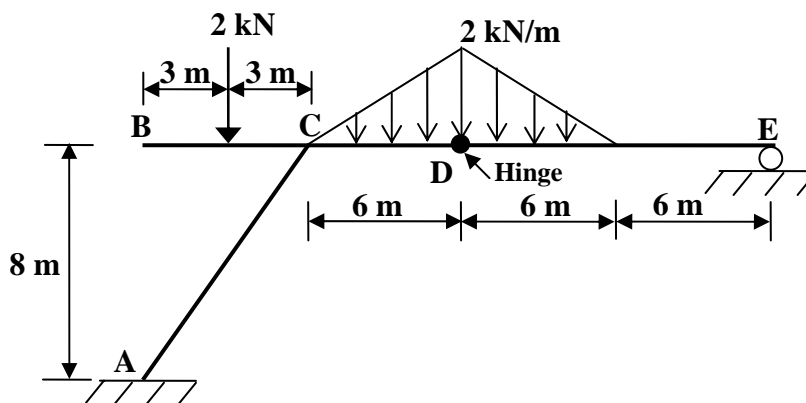
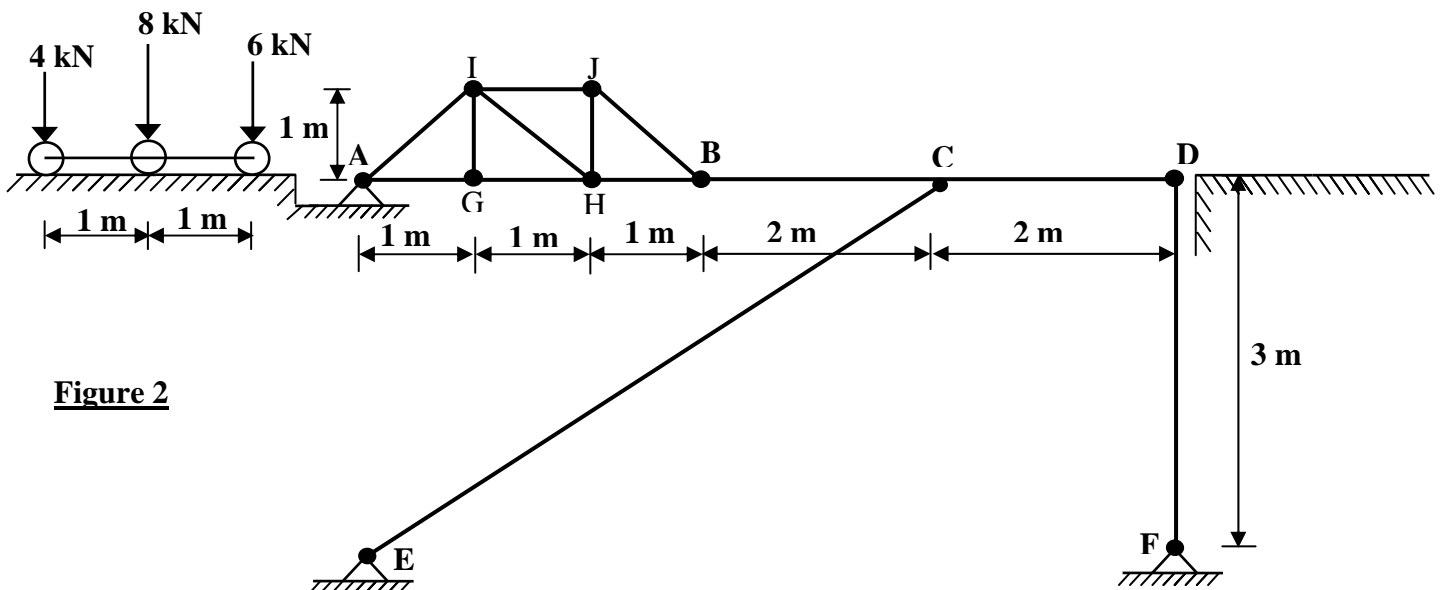
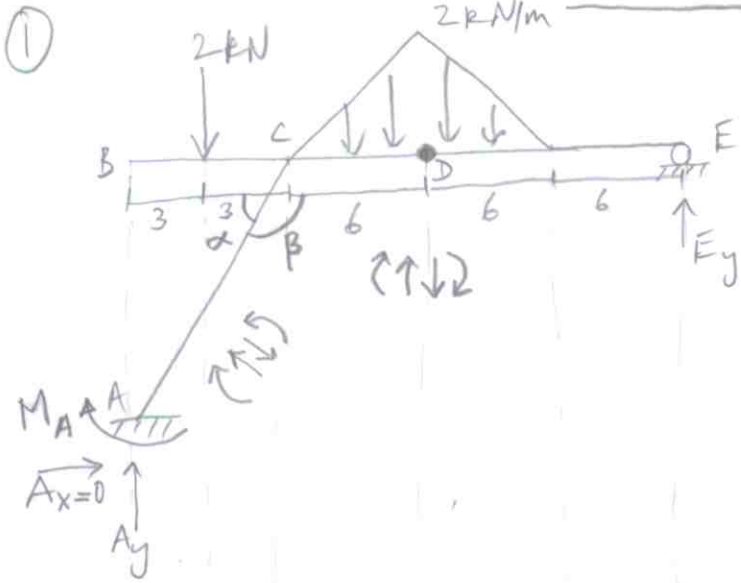


Figure 2



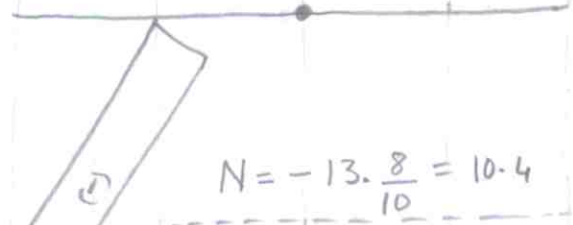


$$\sum M_D = 0 \Rightarrow E_y = \frac{1}{2} \cdot 6 \cdot 2 \cdot 2 = 1 \text{ kN}$$

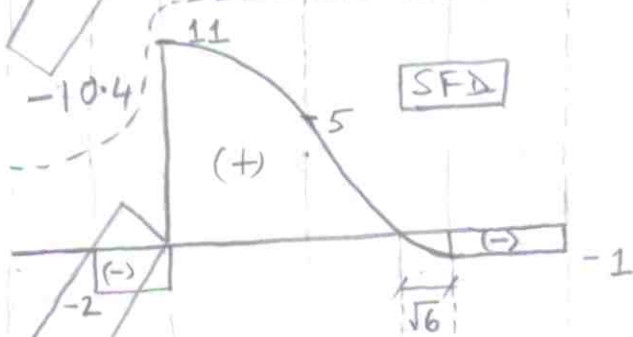
$$\Rightarrow A_y = 2 + \frac{1}{2} \cdot 12 \cdot 2 - 1 = 13 \text{ kN}$$

$$M_A = -(2 \cdot 3 + \frac{1}{2} \cdot 12 \cdot 2 \cdot 12 - 1 \cdot 24) = 126 \text{ kN}\cdot\text{m}$$

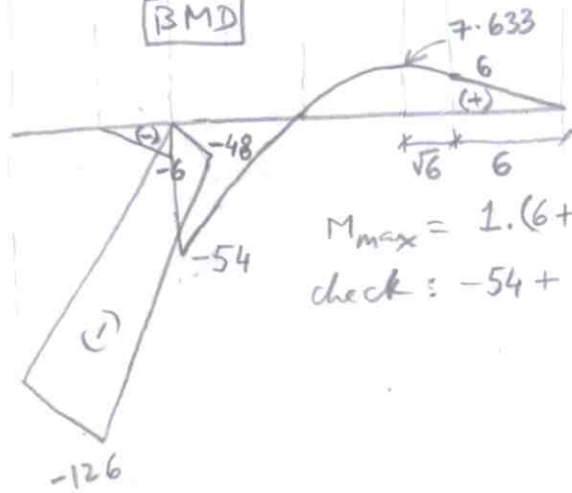
AFD



SFD



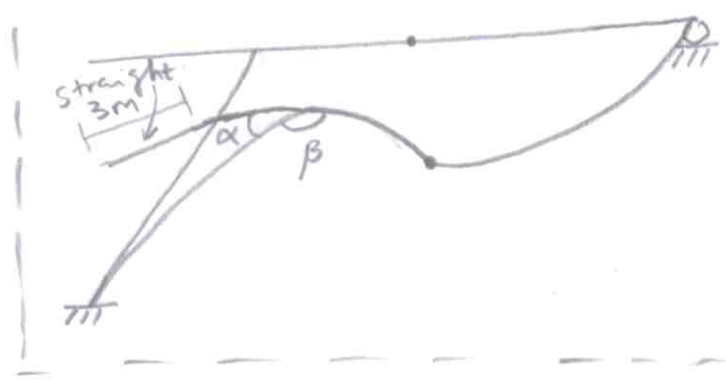
BMD



$$M_{max} = 1 \cdot (6 + \sqrt{6}) - \frac{1}{2} \cdot \sqrt{6} \cdot \frac{\sqrt{6}}{3} \cdot \frac{\sqrt{6}}{3} = 7.633$$

$$\text{check} = -54 + 11 \cdot 6 - \frac{1}{2} \cdot 2 \cdot 6 \cdot \frac{1}{3} \cdot 6 = 0 \text{ (at hinge)}$$

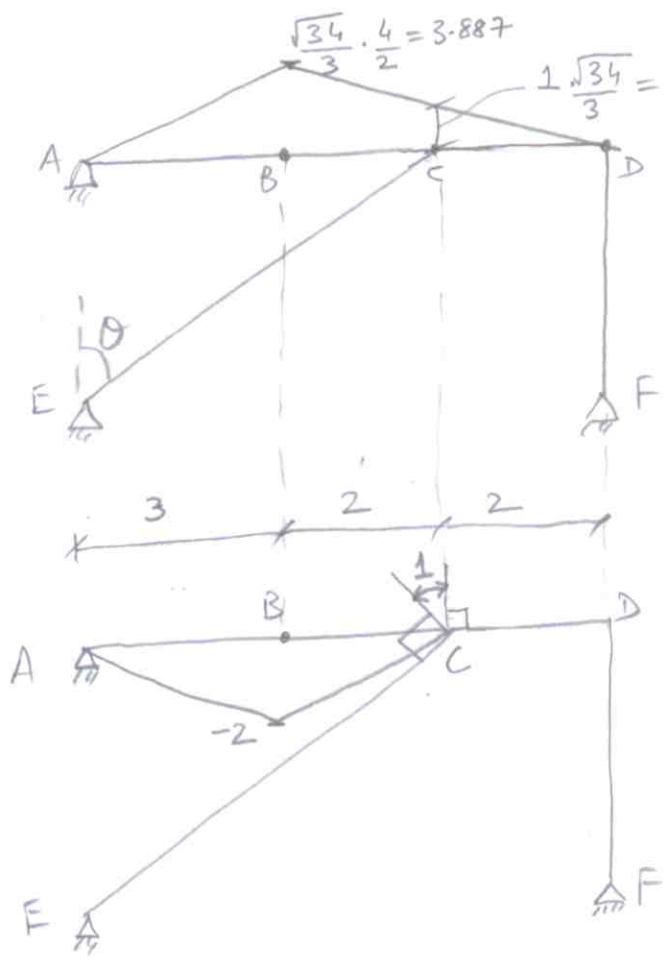
DEFL SHAPE



$$\frac{1}{2} x \cdot \frac{1}{3} x = 1 \Rightarrow x = \sqrt{6} = 2.45$$

②

②



IL-EC (compressive)

Best to use Muller Breslau.
 Release EC (\equiv releasing its vertical component) and give unit⁽¹⁾ displ in vertical direction.
 Then IL-EC at C = $\frac{1}{\cos \theta} = \frac{\sqrt{34}}{3}$
 (maintain support at A, D)

IL- M_c in BCD

Best to use Muller Breslau.
 Create hinge at C, give unit rotational displ, maintain support at A, C, D.

$(EC)_{max}$ when 8kN at B, train moving rightward so that 6kN on shallower slope

$$(EC)_{max} = \frac{\sqrt{34}}{3} \cdot \frac{4}{2} \left(8 + 6 \cdot \frac{3}{4} + 4 \cdot \frac{2}{3} \right) = 58.96 \text{ kN} \blacktriangleleft$$

$(M_c)_{max}$ in BCD when 8kN at B, train moving leftward so that 6kN on shallower slope

$$(M_c)_{max} \text{ in BCD} = -2 \left(8 + 6 \cdot \frac{2}{3} + 4 \cdot \frac{1}{2} \right) = -28 \text{ kN} \blacktriangleleft$$